

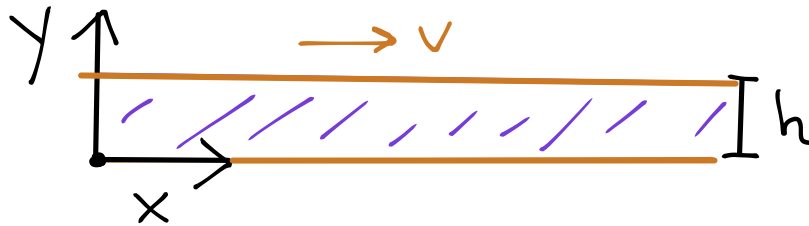
# Biological Hydrodynamics

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Next Tutorial: Thursday **21th November**, 14:50 - 16:20, MPI PKS Seminar Room 3

## Tutorial 4: Couette flow



Consider a layer of an incompressible Newtonian fluid of density  $\rho$  and viscosity  $\eta$  that is placed in between two plates that are separated by  $h$ . The bottom plate is fixed in space, the top plate moves at a velocity  $v$  in the  $x$ -direction. There are no-slip boundary conditions at both plates. Pressure is uniform throughout. All variables do not change in the  $x$  direction.

1. Use the Stokes' equation for low Reynolds numbers to evaluate the velocity profile  $v_x(y)$ .
2. Evaluate the stress tensor. Evaluate the drag force on a square area of extent  $l$  in  $x$ -direction and width  $Z$  that the top plate exerts on the bottom plate. By how much does the drag force decrease if you double the separation distance  $h$ ?
3. What is the drag on the top plate?
4. Calculate the volumetric flow rate  $Q$  (the total volume of fluid per unit time that passes through a cross-section of width  $Z$ ). If you double the separation distance  $h$ , by what factor do you increase  $Q$ ?